

5.32) (a) The Clausius-Clapeyron equation says that the phase boundary obeys  $\frac{dP}{dT} = \frac{L}{T \Delta V}$  (on a P-T diagram)

This explains why the slope  $\frac{dP}{dT}$  is negative: the change in volume when ice changes to water is negative, since the density of ice =  $917 \text{ kg/m}^3$  is lower than that of water, which is  $\approx 1000 \text{ kg/m}^3$ . [Of course, the latent heat  $L$  is a positive quantity due to the increase in entropy as ice  $\rightarrow$  water.]

$$(b) \Delta P = \frac{L}{T} \cdot \frac{\Delta T}{\Delta V} = \frac{333 \text{ kJ}}{273 \text{ K}} \cdot \frac{(-1) \text{ K}}{(1 - (0.917)^{-1}) \times 10^{-3} \text{ m}^3} \quad (\text{for } 1 \text{ kg.})$$
$$= \frac{333}{273} \times \frac{10^6}{0.09051} = 13.5 \times 10^6 \text{ Pa} \approx 135 \text{ atm.}$$

$$(c) P = \rho g h \Rightarrow h = \frac{P}{\rho g} = \frac{13.5 \times 10^6 \text{ Pa}}{(917 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} = 1501 \text{ m.}$$

$$(d) \text{Weight} \approx 80 \text{ kg} \times g \approx 800 \text{ N.}$$

$$\text{Skate area} \approx 25 \text{ cm} \times 0.2 \text{ cm} \approx 5 \times 10^{-4} \text{ m}^2.$$

$$P \approx \frac{800}{5 \times 10^{-4}} = 160 \times 10^4 \approx 16 \text{ atm.}$$

Thus,  $P$  is not enough to depress the melting point.