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$$(a) \quad S = kq \ln \left(1 + \frac{N}{q} \right) + kN \ln \left(1 + \frac{q}{N} \right) \quad [Eq. (2.18)].$$

$$\begin{aligned} \mu &\equiv -T \left(\frac{\partial S}{\partial N} \right)_{u,v} = -T \left(\frac{\partial S}{\partial N} \right)_q = \\ &= -Tk \left\{ q \frac{1/q}{1+N/q} + \ln \left(1 + \frac{q}{N} \right) + \frac{N}{1+q/N} \left(-\frac{q}{N^2} \right) \right\} \\ &= -kT \left\{ \frac{1}{1+N/q} + \ln \left(1 + \frac{q}{N} \right) - \frac{1}{1+N/q} \right\} \\ &= -kT \ln \left(1 + \frac{q}{N} \right). \end{aligned}$$

$$(b) \quad N \gg q \quad \mu = -\frac{kTq}{N}$$

$$\text{Thus, } \Delta S = -\frac{\mu}{T} \cdot \Delta N = \frac{kq}{N} \ll k. \quad \text{when we add 1 particle. This is small!}$$

$$q \gg N, \quad \mu \approx -kT \ln \left(\frac{q}{N} \right)$$

So ΔS is much larger here.

$$\Delta S = -\frac{\mu}{T} \Delta N \approx k \ln \left(\frac{q}{N} \right). \quad \text{when we add a single particle. This is much larger than } \frac{kq}{N} \text{ earlier.}$$

In the second case μ is a more negative number.