

3.20)

$$\text{We have } x = \frac{\mu B}{kT} = \frac{9.27 \times 10^{-24} \text{ J/T} \times 2.06 \text{ T}}{1.38 \times 10^{-23} \text{ J/K} \times 2.2 \text{ K}} = 0.629$$

$$\tanh x = 0.558, \text{ and}$$

$$\frac{U}{U_{\max}} = -\tanh x = -0.558, \text{ while } \frac{M}{M_{\max}} = \tanh x = 0.558.$$

$$\text{Now, } \frac{N_{\uparrow}}{N} = \frac{1}{2} \left(1 - \frac{U}{U_{\max}} \right) = 0.78. \text{ Thus, } \frac{N_{\downarrow}}{N} = 0.22.$$

$$\text{Thus, } \frac{S}{S_{\max}} = \frac{-Nk(x \ln x + (1-x) \ln(1-x))}{-Nk \ln 2} = 0.76.$$

To get to 99% magnetization, i.e., $\tanh x = 0.99$,
 $x = 2.65$.

$$\text{Thus } T \text{ should be } 2.2 \text{ K} \times \left(\frac{2.65}{0.629} \right)^{-1} = 0.52 \text{ K}.$$