2/6/25

Homework Set 1

Instructor: Ralf W. Gothe

1.1) There is Nothing as Certain as the Uncertainty

- 1.1.1) [4] Express at least four uncertainty relations and their meanings!
- 1.1.2) [4] Which color have $2.11 \, eV$ photons and what is the smallest distance they can resolve?
- 1.1.3) [2] What is the smallest distance one can resolve in scattering 6 GeV electrons off a infinitely heavy target?
- 1.1.4) [4] Estimate from the typical size of an atom $(10^{-10} m)$ and a nucleus $(10^{-14} m)$ the needed binding energies! Explain why the results are meaningful even without knowing anything about the underlying forces!

1.2) Spectroscopy with Electromagnetic Fields

- 1.2.1) [4] Show why the magnetic field can be used as a momentum and the electric field as an energy filter!
- 1.2.2) [2] How can you determine the velocity of a particle of unknown but nonzero charge and mass?
- 1.2.3) [3] How can a particle travel on a straight line through a magnetic field? Name at least three scenarios!
- 1.2.4) [2] How can the charge-over-mass ratio of an unknown particle of unknown velocity be determined in a combination of magnetic and electric fields?

1.3) The Hydrogen Atom

- 1.3.1) [3] Rewrite the Coulomb potential energy in terms of α and $\hbar c$ and calculate it for an electron at $r = 0.529 \cdot 10^{-10} \, m$ in a hydrogen atom.
- 1.3.2) [2] Calculate the kinetic energy of an electron localized in such a small spatial volume. [GS] Why is it half the potential energy?
- 1.3.3) [GS] [4] Calculate the potential energy by integrating the electric field energy density from $r = 0.529 \cdot 10^{-10} \, m$ to ∞ .