

6.12) Since there are 3 excited states with energy higher than the ground state of  $\Delta E = 0.47 \text{ meV}$ , we know that

$$\frac{3}{10} = 3 \times e^{-\Delta E/kT}$$

Thus,  $0.1 = e^{-\Delta E/kT}$ . Using  $k = 86 \mu\text{eV}/\text{K}$

and  $T = \frac{-\Delta E}{k \ln(0.1)}$  we get  $T = \frac{-470}{86 \times (-2.303)} = 2.38 \text{ K}$ .

This is close to the cosmic "furnace" temperature of 2.7 K : this is how cold the "universal oven" has become after the fiery big bang 13.8 billion years ago.