

20.(a) We will adopt the summation convention and drop the summation signs:

$\epsilon_{ijk} \delta_{ij}$  is a "contraction of an antisymmetric and symmetric object".

$\delta_{ij}$  is non-zero (1) only when  $i=j$  and that's when  $\epsilon_{ijk} = 0$ . Thus, every term in the sum is zero and the sum is zero.

(b)  $\epsilon_{ijk} \epsilon_{ijk}$  for given values of  $i$  and  $l$  are non-zero only when  $j$  and  $k$  are both unequal to both  $i$  and  $l$ . Since all these indices can only have 3 values, non-zero products only arise when  $i=l$ . In that case there are 2 possible values for  $j, k$ ; in both cases  $\epsilon_{ijk}^2 = 1$  and we get a sum of products equal to 2. Of course, when  $i \neq l$  we get zero. Thus,  $\epsilon_{ijk} \epsilon_{ijk} = 2\delta_{il}$ .

(c) Summing the above over the 3 possible values of  $i$  gives us 3 times the earlier result of 2:

$$\epsilon_{ijk} \epsilon_{ijk} = 3 \times 2 = 6.$$